

Can we predict ENSO using a simple model?

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1) Introduction

- Question: Can we simulate and predict the irregular oscillation of ENSO?

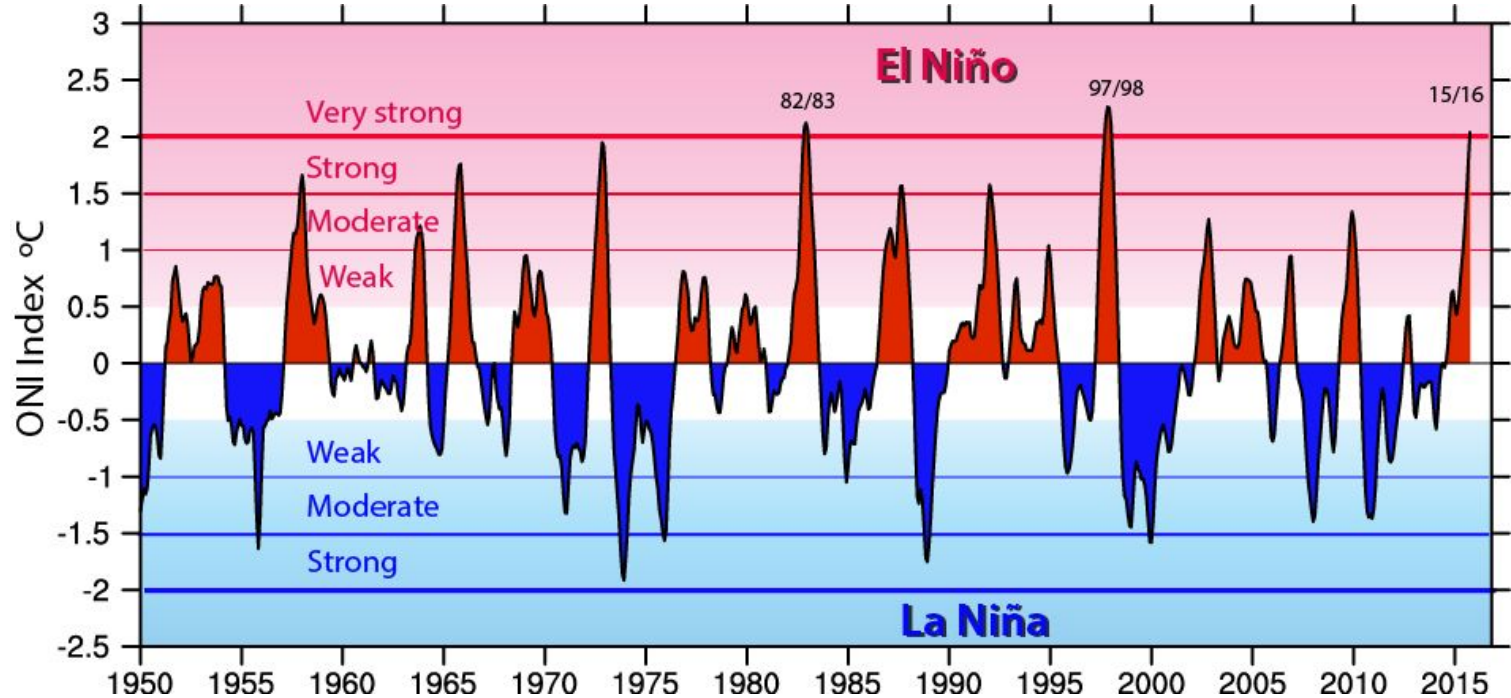


Fig. 1: ENSO index (Source: NCAR)

2) ENSO Recharge oscillator

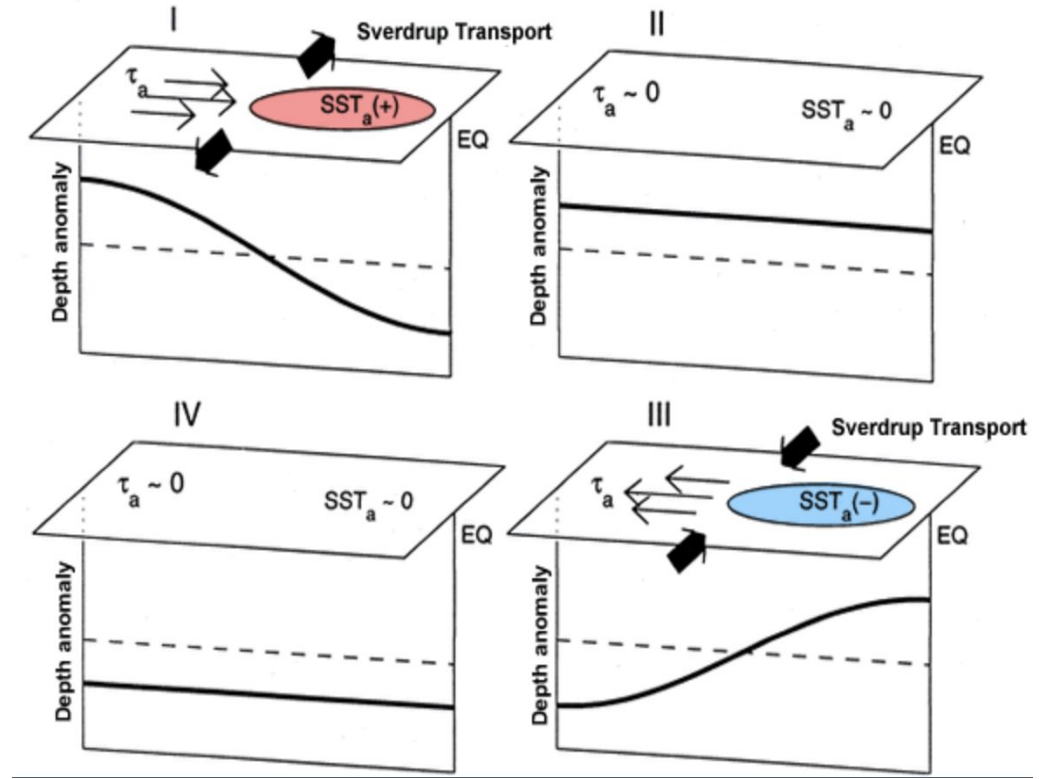
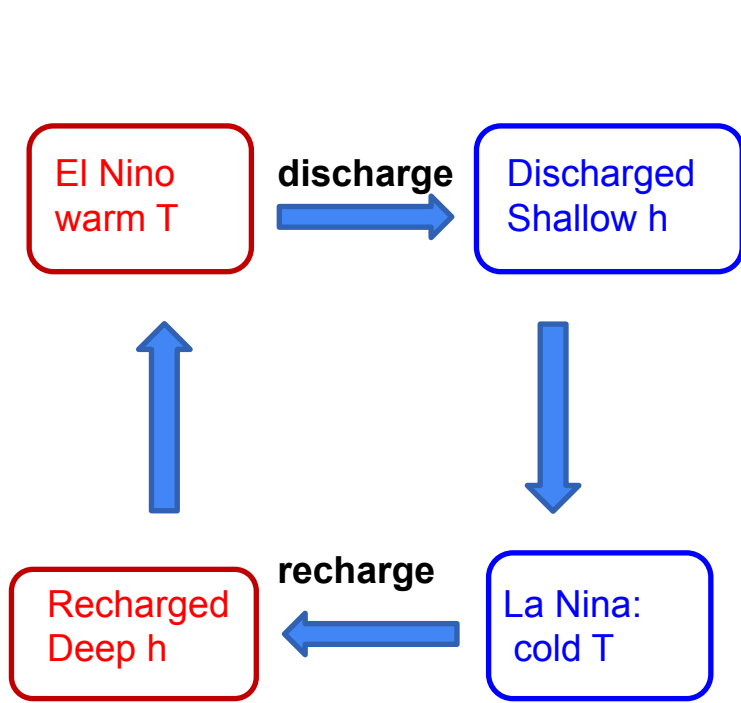


Fig. 2: Recharge-discharge mechanism (Meinen & McPhaden, 2000)

3) A conceptual model

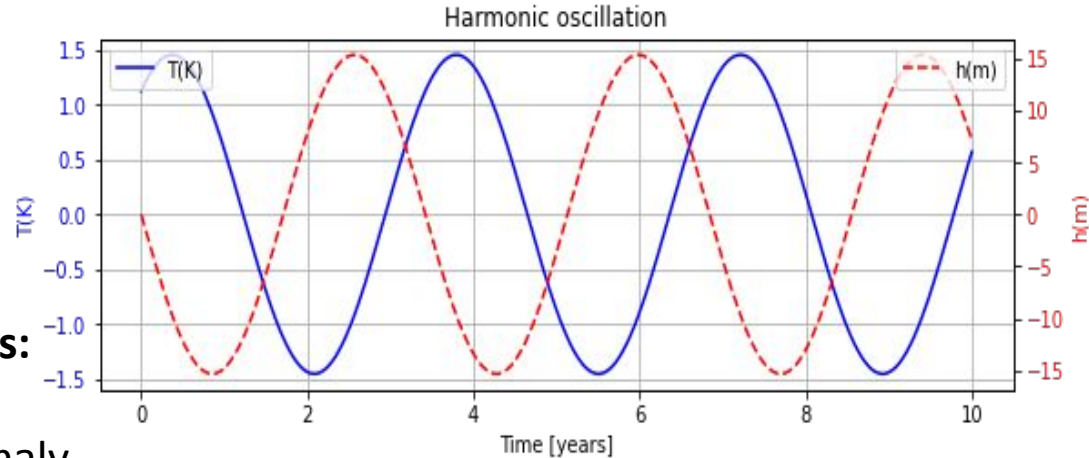
$$\frac{dT}{dt} = RT + \gamma h \quad (1)$$

$$\frac{dh}{dt} = -rh - \alpha b T$$

- **Coupled equations with two variables:**

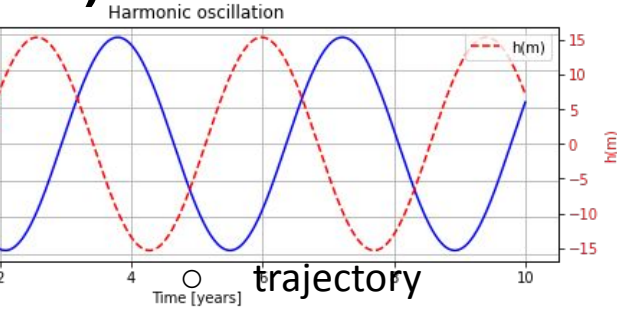
- T : East Pacific SST anomaly
- h : West Pacific thermocline anomaly

- R : Growth rate of T
- γ : Coupling of T to h
- r : Damping rate of h
- αb : Coupling of h to T



- How do we decide each parameters value?
 - based on statistic regression from observation data
- How to solve equations numerically?
 - Runge Kutta 4th
 - Time step: 1 day

4) Model results:



- Bad things:
 - Unstable if strongly coupled
 - Decays if weakly coupled
 - Pattern is regular
 - Period is fixed

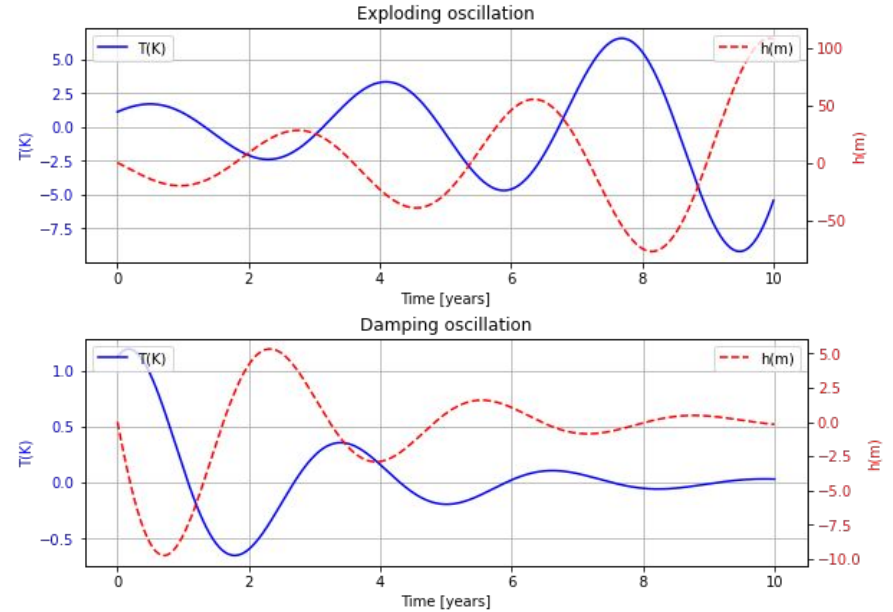


Fig. 3: Numerical solutions with varying coupling intensity

- **Add nonlinearity:**

- Nonlinear dependence of T on h

$$\frac{dT}{dt} = RT + \gamma h - \epsilon(h + bT)^3 \quad (2)$$

$$\frac{dh}{dt} = -rh - \alpha bT$$

- **Add wind stress:**

- Annual cycle wind

$$\frac{dT}{dt} = RT + \gamma h - \epsilon(h + bT)^3 + \gamma \xi$$

$$\frac{dh}{dt} = -rh - \alpha bT - \alpha \xi$$

$$\xi = f_{ann} \cos\left(\frac{2\pi t}{\tau}\right)$$

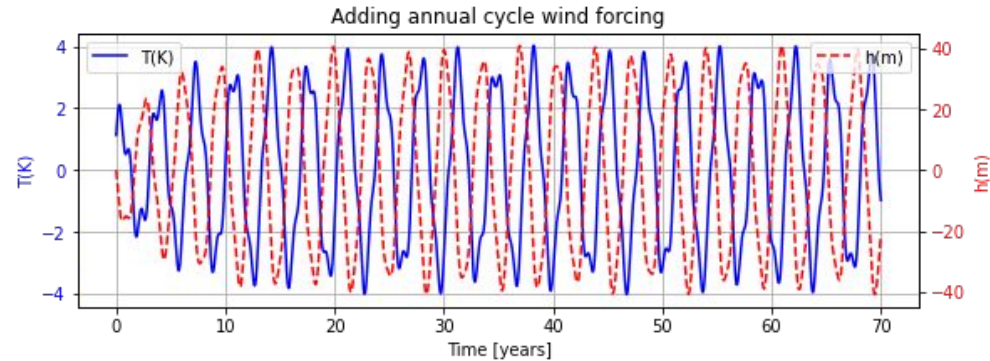
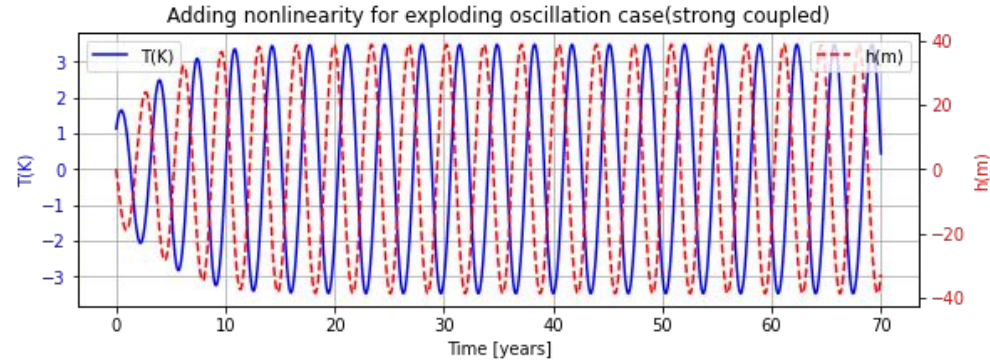


Fig. 4: Numerical solutions after adding nonlinearity (above) and both nonlinearity and annual cycle wind forcing (below)

Stochastic Forcing

$$\xi = f_{ann} \cos\left(\frac{2\pi t}{\tau}\right) + f_{ran} W \frac{\tau_{cor}}{\Delta t} \quad (4)$$

White noise

$$\begin{aligned} x_1 &= w_1 \\ x_{j+1} &= rx_j + (1 - r^2)^{1/2} w_{j+1}, j \geq 1 \end{aligned} \quad (5)$$

Red noise

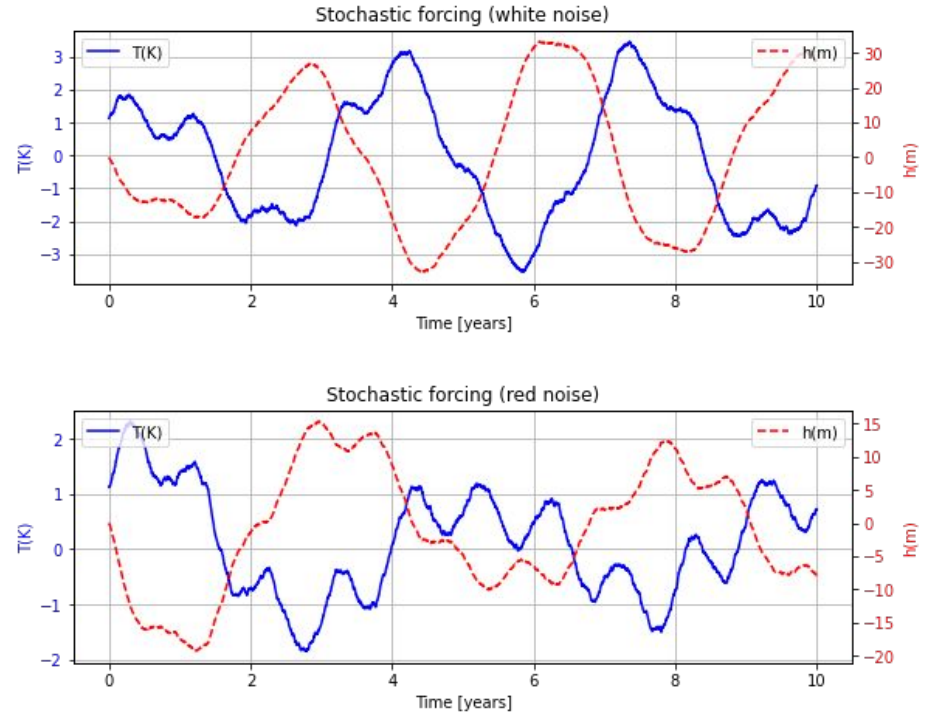
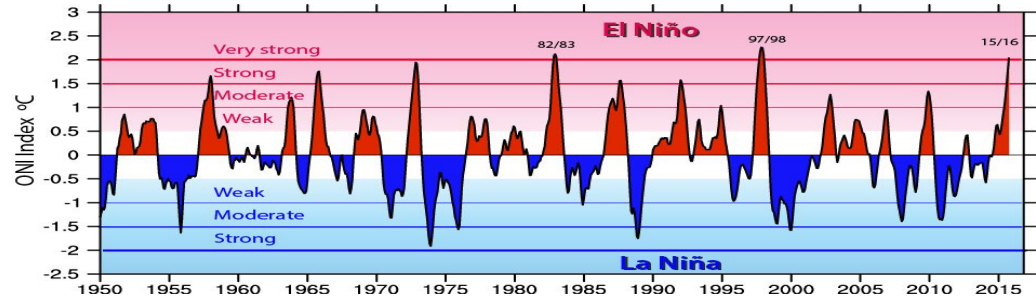


Fig. 5: Numerical solutions with white noise (above) and red noise (below)

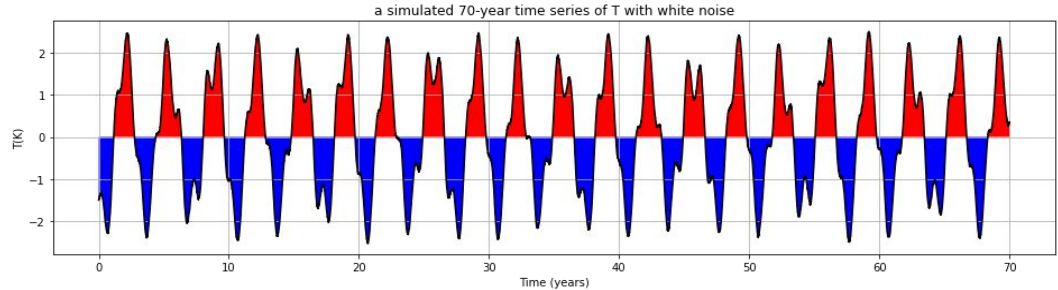
Observed

- ONI, ~70 years



White noise

- Period and amplitudes are (too) uniform
- More events than observed



Red noise

- More chaotic
- Correct no. of events
- Period and amplitudes less uniform

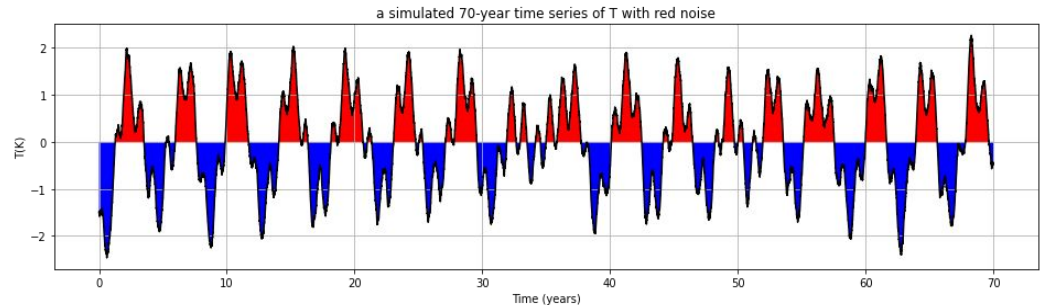


Fig. 6: 70-year time series of ONI and model data

Ensemble Model (Red Noise)

Steady oscillation

Not sensitive to initial conditions

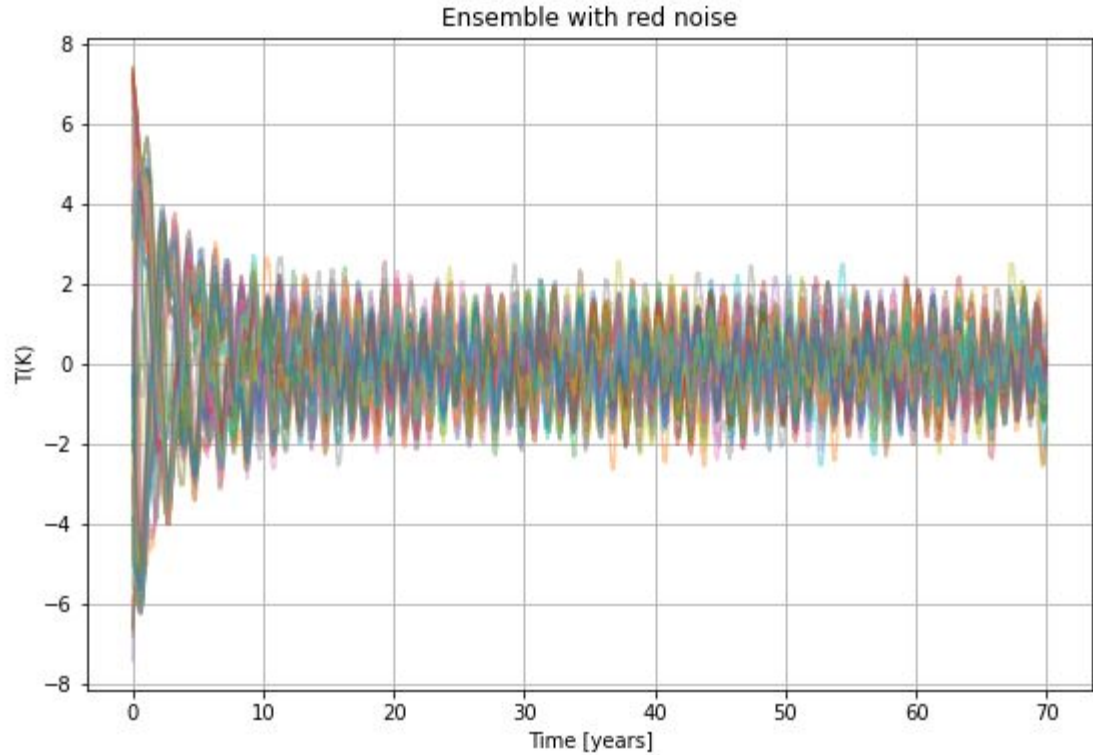


Fig. 7: Ensemble with red noise (70 years).

Comparison of Ensemble with Reality

Grey: white noise
Red: red noise
Blue: NINO34 data

Model matches observations

Note spread of white noise

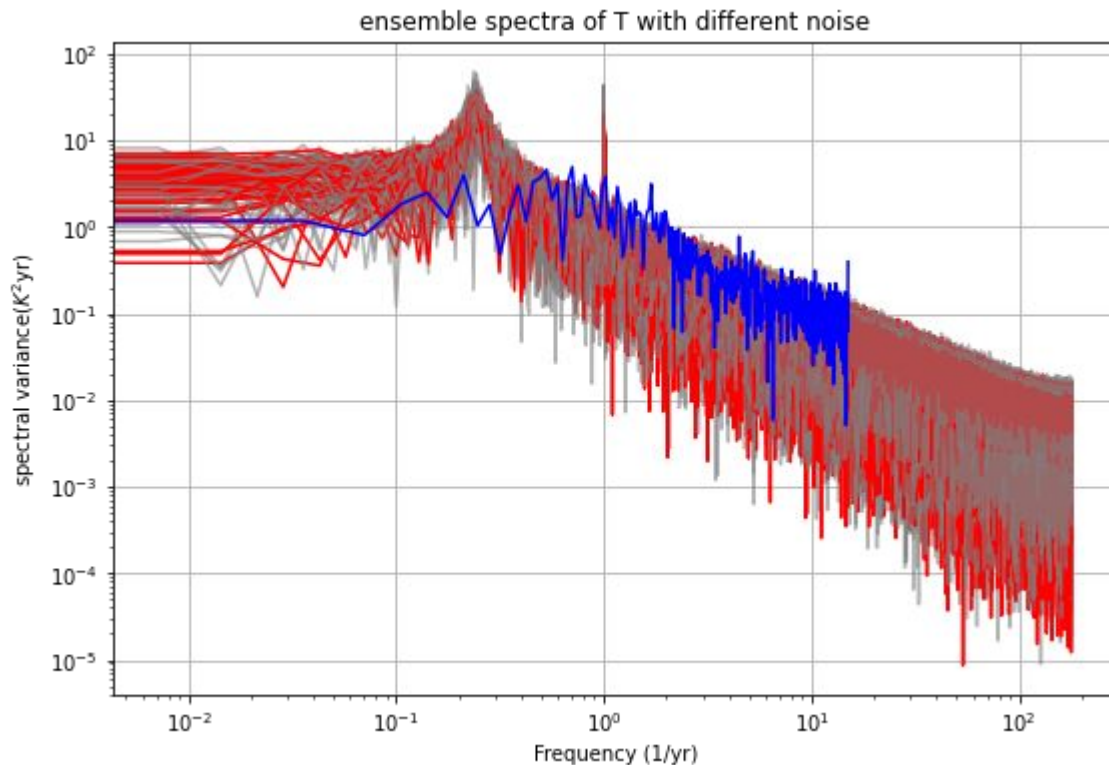


Fig. 8: Fourier spectra for real ENSO and model with white/red noise

5) Summary and Discussion

$$\begin{aligned}\frac{dT}{dt} &= RT + \gamma h \\ \frac{dh}{dt} &= -rh - \alpha bT\end{aligned}\tag{1}$$

- Model is a coupling between thermocline height and SST.
- Model simulates key features
 - Period, duration, amplitude, trajectory
- Nonlinearity and red noise are important
- ENSO predictable on short timescales
- Simple, old model. More complex interpretations now. [See Timmerman et al, 2018]



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